

UNIVERSITY OF IOANNINA PHYSICS DEPARTMENT NUCLEAR PHYSICS LABORATORY



Study of the ¹⁶²Er(n,2n)¹⁶¹Er reaction at near threshold energies

M.Sc. Thesis Efstathia Georgali

Academic supervisor: Nikolas Patronis

Ioannina, February 2017



ΠΑΝΕΠΙΣΤΗΜΙΟ ΙΩΑΝΝΙΝΩΝ ΤΜΗΜΑ ΦΥΣΙΚΗΣ ΕΡΓΑΣΤΗΡΙΟ ΠΥΡΗΝΙΚΗΣ ΦΥΣΙΚΗΣ



Μελέτη της αντίδρασης 162 Er(n,2n) 161 Er κοντά στο ενεργειακό κατώφλι

ΜΕΤΑΠΤΥΧΙΑΚΗ ΔΙΠΛΩΜΑΤΙΚΗ ΕΡΓΑΣΙΑ

Ευσταθία Γεωργαλή

Ακαδημαϊκός επιβλέπων : Νικόλας Πατρώνης

Ιωάννινα, Φεβρουάριος 2017

Ευχαριστίες

Θα ήθελα να εκφράσω την ευγνωμοσύνη μου στον Επ. Καθ. Νικόλα Πατρώνη του Τμήματος Φυσικής, του Πανεπιστημίου Ιωαννίνων, που επέβλεψε αυτή την εργασία. Κατ' αρχάς του χρωστάω ένα μεγάλο ευχαριστώ για την εμπιστοσύνη που μου έδειξε και για την ευκαιρία που μου προσέφερε να δουλέψω πάνω σε αυτό το κομμάτι της Πυρηνικής Φυσικής, που λέγεται Πυρηνικές Αντιδράσεις. Ακόμη, θέλω να τον ευχαριστήσω για τον ενεργό ρόλο και τη προθυμία του να βοηθήσει σε όλες δυσκολίες της πειραματικής ανάλυσης, αλλά και για τις γνώσεις που με βοήθησε να αποκομίσω από αυτόν.

Ακόμη, θέλω να ευχαριστήσω την φίλη και συναδελφό μου Ζηνοβία Ελεμέ, επίσης μεταπτυχιακή φοιτήτρια του Τομέα Πυρηνικής Φυσικής, του Τμήματος Φυσικής, του Πανεπιστημίου Ιωαννίνων. Την ευχαριστώ για την βοήθεια της στη διεκπεραίωση αυτής της εργασίας, για τις εποικοδομητικές συζητήσεις που κάναμε μαζί πάνω σε ζητήματα της πειραματικής ανάλυσης αλλά και για τις όμορφες στιγμές που είχαμε δουλεύοντας μαζί.

Acknowledgements

I would like to express my gratitude to Assistant Prof. Nikolas Patronis, who supervised this thesis. First of all, I owe him a thank you for the confidence he showed me and the opportunity he gave me to work on this part of Nuclear Physics, called Nuclear Reactions. Moreover, I want to thank him for his active part and willingness to help in every experimental analysis difficulty, but also for the knowledge he helped me to derive from him.

Moreover, I want to thank my friend and colleague Zinovia Eleme, also being a postgraduate student at the Nuclear Physics Laboratory at the Physics Department of the University of Ioannina. I thank her for her assistance to the prosecution of this study, the constructive conversations we had on experimental analysis issues and the beautiful time we had working together.

Περίληψη

Η ενεργός διατομή της αντίδρασης ¹⁶²Er(n,2n)¹⁶¹Er προσδιορίστηκε πειραματικά με την τεχνική της ενεργοποίησης για τρεις ενέργειες δέσμης νετρονίων κοντά στο ενεργειακό κατώφλι. Ο προσδιορισμός της ενεργούς διατομής έγινε σε σχέση με τις αντιδράσεις αναφοράς: ¹⁹⁷Au(n,2n)¹⁹⁶Au, ⁹³Nb(n,2n)^{92m}Nb και ²⁷Al(n,α)²⁴Na. Η ημί-μονό-ενεργειακή δέσμη νετρονίων παράχθηκε μέσω της αντίδρασης ²H(d,n)³He στον επιταχυντή Tandem Van der Graaf 5.5 MV του Ινστιτούτου Πυρηνικής και Σωματιδιακής Φυσικής του Ε.Κ.Ε.Φ.Ε "Δημόκριτος",χρησιμοποιώντας αέριο στόχο δευτερίου. Μετά το τέλος κάθε ακτινοβόλησης πραγματοποιήθηκε η μέτρηση της ενεργότητας των δειγμάτων. Λόγω της ελάχιστης περιεκτικότητας του στόχου Ερβίου σε ¹⁶²Er για τις μετρήσεις της ενεργότητας χρησιμοποιήθηκαν δύο ανιχνευτές γερμανίου HPGe με σχετική απόδοση 16%. Από την παρούσα εργασία προέκυψαν τα πρώτα πειραματικά δεδομένα για τις εξής ενέργειες δέσμης νετρονίων : 10.7 MeV, 11.0 MeV και 11.3 MeV.

Abstract

The ¹⁶²Er(n,2n)¹⁶¹Er reaction cross section was experimentally determined by means of the Activation Technique relative to the ¹⁹⁷Au(n,2n)¹⁹⁶Au, ⁹³Nb(n,2n)^{92m}Nb and ²⁷Al(n, α)²⁴Na reference reactions at near threshold energies. The quasi-mono-energetic neutron bean was produced via the ²H(d,n)³He reaction at the 5.5 MV Tandem Van der Graaf accelerator of the Institute of Nuclear and Particle Physics at N.C.S.R. "Demokritos", using gas deuterium target. After each irradiation, the targets' induced activity was measured. Due to the minimal abundance of ¹⁶²Er in the natural erbium target for the activity measurements two 100% relative efficiency HPGe detectors were used in close geometry, whereas for the activity measurements of the reference foils one 16% HPGe detector was used. From the present work the ¹⁶²Er(n,2n)¹⁶¹Er reaction cross section was determined for the first time at the following neutron beam energies : 10.7 MeV, 11.0 MeV and 11.3 MeV.

Contents

Ευχαριστίες	
Acknowledgements	
Περίληψη	
Abstract	
1. Introduction	14
1.1 Motivation	14
1.2 Previous experimental data of the ¹⁶² Er(n,2n) ¹⁶¹ Er reaction cross section	15
1.3 Nuclear Reaction Mechanisms	16
1.4 The ¹⁶² Er+n interaction	17
1.5 Energy Diagram of the ¹⁶² Er+n interaction	18
2. Experimental Set-up and Method	20
2.1 Activation Technique	20
2.2 Erbium target and reference foils	22
2.3 Neutron beam	24
2.4 Neutron beam fluctuations and BF_3 Detector	26
2.5 Irradiation Set-up	28
2.6 γ -ray Detectors	29
2.7 Detectors calibration	31
3. Data Analysis	33
3.1 Calibration curves of the 16% HPGe Detector	33
3.2 Reference foils' efficiency	36
3.3 2x100% HPGe Detectors' efficiency	37
3.4 Activity Measurements	

3.4.1 Reference foils activity measurements
3.4.2 ¹⁶¹ Er Activity
3.5 Correction factors
3.5.1 Decay during irradiation-correction factor50
3.5.2 Self-Attenuation Correction factor
3.5.3 Dead-Time Correction factor52
3.6 Reference reactions Cross Sections
3.7 Neutron Flux53
4. Results
5.Conclusions
Appendix A The Cross Section equation56
Appendix B Decay during irradiation correction factor calculation program in C++ code
Appendix C Geant4 MC simulation code for self-attenuation correction factor
References75
Bibliography75

1. Introduction

1.1 Motivation

The experimental and theoretical study of nuclear reactions cross sections is one of the primary goals of the nuclear physics research. Investigation on nuclear reaction mechanisms contributes not only to a better understanding of the nuclear reactions models and the role of nuclear structure, but also to the development and improvement of many applications.

Within the present work the experimental study of the ${}^{162}\text{Er}(n,2n)^{161}\text{Er}$ reaction is presented. Neutron induced nuclear reactions with rare earth elements are in general of special interest for basic research purposes as well as for the development of nuclear physics applications. ${}^{162}\text{Er}$ is the lightest Erbium isotope with minimal abundance (0.139 %). Although, ${}^{162}\text{Er}$ is a stable isotope still is a proton rich nucleus quite far from the mainstream of the valley of stability. Accordingly, its determination of cross section will help for a better understanding of Compound Nucleus reaction theory and its decay mechanisms. Moreover, the exact knowledge of the experimental values of the cross section will help for the determination of the semi-empirical parameters of the Hauser-Feschbach theory equations which are necessary for the theoretical estimations. This procedure will improve the theoretical models and will demonstrate the most suitable ones for the forecast of similar reactions cross sections for nuclei in the this region of the chart of nuclides.

Moreover, nuclear reactions of Erbium isotopes are important due to their high neutron capture cross sections. This fact makes Erbium one of the best materials to be used as neutron absorber in fast neutron reactors [1]. The fast neutron reactors differ with the conventional ones in the fact that they do not use any moderator (commonly water) to slow down the neutrons produced from fission so as to sustain the nuclear chain reaction. In contrast they operate at fast neutron energies. Recently, fast neutron reactors seem to gain their old fame and be a promising technology for power production because of their three major advantages [2]:

- they can solve the problem of "fuel shortage" as they permit fuel to be bred from almost all the actinides. On average, more neutrons per fission are produced from fissions caused by fast neutrons than from them caused by thermal neutrons. This results in a larger surplus of neutrons beyond those required to sustain the chain reaction. These neutrons can be used to produce extra fuel (fast breeder reactors FBR).
- Fast neutron reactors are also effective to burn the long-lived minor actinides of radioactive waste. Actinides have a higher fission cross section at fast energies than at thermal energies. After fission actinides become a pair of "fission products", which have decreased half-life time from some million years to a few centuries.
- Generally, neutron capture rates are lower as the energy of neutron is increased. Therefore, the transuranic radio-toxicity of the produced nuclear wastes is significantly reduced.

1.2 Previous experimental data of the 162 Er(n,2n) 161 Er reaction cross section

Concerning the EXFOR data base the 162 Er(n,2n) 161 Er reaction has been unexplored for a wide energy range, since the only existing experimental data are limited in the energy range between 13.5-15 MeV ([3]-[11]). This inhibits the accurate benchmarking of the theoretical calculations. Things are made even more difficult because of the discrepancies between the experimental data which approach even the 30 %. So, it can be said that the 162 Er(n,2n) 161 Er reaction is still in a primitive stage of study.



Within the present work the measurement of the ${}^{162}\text{Er}(n,2n){}^{161}\text{Er}$ reaction cross section at energies just above the threshold (Q_{th} =9.262 MeV) is presented. According to our knowledge the experimental data of the present work are the first data in this energy region.

1.3 Nuclear Reaction Mechanisms

The nuclear reactions are classified into categories according to the mechanisms of interaction between the projectile and the target-nucleus [12] :

- Direct reactions
- Compound Nucleus reactions

The Direct reactions are peripheral reactions, due to the fact that the projectile, primarily, interacts with the nucleons in the surface of the target-nucleus. In this case the interaction takes place quickly in a time scale of 10^{-22} s. This time is not enough for the projectile to lose its entire energy, but only a portion of it is shared among the target's peripheral nucleons. Due to their small duration and the partial decrease in the projectile's energy, the products of these reactions are strongly depend on the interacting nuclei.

Direct Reactions are classified into four subcategories:

- 1. Elastic scattering: In this case the nucleons are not exchanged between the projectile and the target nuclei. Only the kinetic energy of the projectile and its emission angle are changed.
- 2. Inelastic scattering: In this case also there is no exchange of nucleons . However, part of the kinetic energy is transferred to the bound nucleons exciting the colliding nuclei..
- 3. Stripping reactions: some nucleons are transferred from the projectile to the target.
- 4. Pick up reactions: it is the opposite procedure. In this case the nucleons are transferred from the target to the projectile.

On the other hand, in Compound Nucleus reactions, the projectile interacts with the whole nucleus. The projectile's energy is shared among all the nucleons of the target via nucleons-nucleons reactions, until thermodynamical equilibrium is reached. This means that the projectile is absorbed by the target-nucleus until a compound, highly excited nucleus with lifetime equal to $t \simeq 10^{-16}$ is formed. In other words the projectile loses its " identity " and the compound nucleus may be said that have lost memory of the particular input channel of formation. The compound nucleus is in an excited state and de-excites ("evaporates") in a way that doesn't depend on the input channel. This principle is called Bohr hypothesis. Bohr' hypothesis mathematical formalism is:

$$\sigma_{ab} = \sigma_{\alpha C} G_b$$
 (eq. 1.1)

where, σ_{aC} describes the cross section of the formation of the compound nucleus and G_b its decay probability. The term G_b is expressed as the quotient of the partial decay width:

$$G_b = \frac{\Gamma_b}{\Gamma}$$
 (eq 1.2)

The intermediate mechanism between the two extremes (compound nucleus and direct reactions) are the pre-equilibrium reactions . In these reactions during the nucleon-nucleon interactions, some nucleons or light nuclei acquire enough energy to escape from the complex system target-projectile before the equilibrium is reached. Due to this, there is not total independence between the formation and de-excitation of the target-projectile complex system, but the Compound nucleus "conserves some memory".

Compound Nucleus reactions vs Direct reactions

Although there are no strict boundaries between the direct and the compound reaction mechanisms, the primary parameter that finally determines the mechanism of the reaction is the center-of-mass kinetic energy. Compound Nucleus reactions are favored in lower energies, whereas Direct reactions is the dominant reaction mechanism at higher energies. More specifically, the lower the energy is the larger the wave-length λ of the particle will be (λ =h/p). So, it is easier for the projectile to interact with the whole target and a Compound nucleus to be formed. Respectively, for higher energies the wave-length of the projectile is smaller limiting the interaction with only some peripheral nucleons of the target. It is obvious that the pre-equilibrium reaction mechanism regime are the intermediate energies. This is the reaction that bridges the two extreme cases of nucleus-nucleus interaction.

1.4 The ¹⁶²Er+n interaction

The $^{\rm 162}{\rm Er}$ +n interaction is dominated by the compound nucleus reaction mechanism, which leads the formation of the $^{\rm 163}{\rm Er}^*$ nucleus.

Following the compound nucleus formation in the table given below the different reaction channels are presented:

output channels	Q-value (MeV)		
¹⁶² Er+n	0	elastic scattering	
¹⁶¹ Er+2n	-9.20	endothermic	
¹⁶⁰ Er+3n	-16.41	endothermic	
¹⁵⁹ Er+4n	-25.99	endothermic	
¹⁶² Ho+p	0.49	exothermic	
¹⁶¹ Ho+n+p	-6.43 endothermi		
¹⁵⁹ Dy+α	8.48 exothermic		
¹⁵⁸ Dy+n+α	1.65 exothermic		
¹⁶¹ Ho+d	-4.2	endothermic	
¹⁶⁰ Ho+t	-6.83	endothermic	

Table 1.1: possible output channels of the ¹⁶²Er +n compound nucleus reaction

where Q-value is the energy absorbed (endothermic reaction) or released (exothermic reaction) during the reaction $\$

$$Q(MeV) = \Delta(reactive nuclei) - \Delta(product nuclei)$$
 (eq. 1.3)

whereas Δ is the total mass excess of the initial and product nuclei.

1.5 Energy diagram of the ¹⁶²Er+n interaction

The $^{163}\rm{Er*}$ nucleus is a compound nucleus , which is produced from the $^{162}\rm{Er+n}$ interaction in a high excited state with excitation energy E_x :

$$E_x = S_n + E_{n, CMS} \pmod{1.4}$$

where S_a is the neutron binding energy in the ¹⁶³Er* nucleus and $E_{n,CMS}$ is neutron beam energy (bombarding energy) at the Center of Mass (CM) System

The neutron binding energy is given from the equation:

$$S_n = \Delta(^{162}Er) + \Delta(n) - \Delta(^{163}Er) \Rightarrow S_n = (-66.33 \, MeV) + (8.07 \, MeV) - (-65.17 \, MeV) V \Rightarrow S_n = 6.90 \, MeV$$
(eq 1.5)

The CM neutron energy depends on the laboratory neutron beam energy via the equation:

$$E_{n,CMS} = \frac{A_{RN}}{A_{CN}} E_{Lab} \quad (eq. 1.6)$$

where A_{RN} is the mass number of the target nucleus (A_{RN} =162) and A_{CN} is the mass number of the compound nucleus (A_{CN} =163).

Consequently, for the three irradiations:

En (MeV) at lab	Е _{п,СМS} (MeV)
10.7	10.6
11.0	10.9
11.3	11.2

Table 1.2: neutron beam energies at CMS for each irradiation

and the excitation energies for each irradiation are:

En (MeV)	excitation energy (MeV)
10.7	17.5
11.0	17.8
11.3	18.1

<u>Table 1.3</u>: excitation energies of ¹⁶³Er* compound nucleus for each irradiation energy

According to the information with respect to the excitation energy of the compound nucleus as presented previously and the required energy for each reaction channel as presented below, the energy

output channels	energy levels (MeV)		
¹⁶² Er+n	6.90		
¹⁶¹ Er+2n	16.10		
¹⁶⁰ Er+3n	23.31		
¹⁵⁹ Er+4n	32.89		
¹⁶² Ho+p	6.41		
¹⁶¹ Ho+n+p	13.33		
¹⁵⁹ Dy+α	-1.58		
¹⁵⁸ Dy+n+α	5.25		
¹⁶¹ Ho+d	11.10		
¹⁶⁰ Ho+t	13.73		

diagram of the $n+^{162}$ Er reaction can be formed (Figure 1.2).

<u>Table 1.4</u>: the possible reaction channels of the interaction between the $^{\rm 162}{\rm Er}$ and the neutron in accordance with the $^{\rm 163}{\rm Er}^*$ level.

Where for the energy level determination it was applied the equation:

 $Q(MeV) = \Delta(^{163}Er) - \Delta(reactive nuclei)$ (eq. 1.7)

Here the term Q corresponds to the excitation of the compound nucleus ¹⁶³Er* for zero beam energy.



Figure 1.2: enery diagram of the ¹⁶²Er+n interaction

2. Experimental Set-up and Method

2.1 Activation Technique

The Activation Technique is an established technique for the determination of the reaction cross section. The high sensitivity and selectivity of the method has been proven [13]. This method can be implemented in those physics cases where the product nucleus of the reaction under study is an unstable nucleus with suitable decay parameters (intensity, energy, decay mode, half-life, etc) [14]. More specifically, the activation technique consists of two stages: Firstly, the sample-target is irradiated by mono-energetic particle-beam. The target material as well as the particle beam depends on the reaction under study. During the irradiation the unstable product nuclei are formed. After the irradiation the induced activity with respect to the population of the product nucleus of the reaction under study is measured. Accordingly, the cross section can be obtained using the following equation.:

$$\sigma = \frac{A CF_{SA} CF_{DT}}{N_T \Phi \varepsilon I_{\gamma} (1 - e^{-\lambda t_m}) e^{-\lambda t_w} f_b} \quad (\text{eq } 2.1)$$

where A, the induced daughter's nucleus Activity

- Φ , the irradiation flux
- N_{T} , the initial number of stable nuclei in the irradiation sample
- I, the emitted ray's intensity
- $\boldsymbol{\epsilon}, \mbox{ detector's efficiency for the emitted radiation }$
- λ , the decay constant of the daughter nucleus
- t_m, the measuring time of the induced activity

 t_w , the waiting time between the end of the irradiation and the start of measurement

 CF_{SA} , the sample's self-attenuation correction factor

 CF_{DT} , the detector's dead time correction factor

 f_b , the correction factor for the daughter nuclei decay during irradiation

For constant flux:
$$fb = \frac{(1 - e^{-\lambda t_{ir}})}{\lambda t_{ir}}$$
 (eq. 2.2), whereas for non-constant flux: $fb = \frac{\int_{0}^{t_{ir}} f(t)e^{\lambda t}dt}{\int_{0}^{t_{ir}} f(t)}e^{-\lambda t_{ir}}$ (eq. 2.3)

After the irradiation the population of the reaction product has to be determined. Therefore, for the daughter nucleus activity off-line measurements are conducted. This sets a limit to the application of the Activation Technique. More specifically, the daughter nucleus half-life time has to be long enough. This ensures that the nuclei will not decay just after the irradiation stops, before the activity measurement takes place. However, the half-life time cannot be very long as well. In such a case, a long irradiation and measuring time are necessary for achieving a reasonable decay rate and to obtain a sufficiently adequate statistics.

The off-line measurements, despite the afore mentioned limitations with respect the decay characteristics, have an important advantage. Given that the off-line measurements is free from any

beam-related background results in significant improved signal-to-background ratio thus increasing the selectivity and sensitivity of the measurement.

Another consideration when Activation Technique is applied, is the absence of interference reactions. Before applying the Activation Technique it has to be ensured that there are no reactions producing the same isotope as the one being populated by the reaction of interest.

The equation (2.1) combines three magnitudes: the cross section σ of the reaction under study, the irradiation flux Φ and the number of target nuclei N_T . This means that if two of the three are known each time, the third can be easily calculated. Usually, the final goal of an experiment is the reaction cross section determination.

The number of the target nuclei in the sample $N_{\scriptscriptstyle \rm T} {\rm is}$ equal to:

$$N_T = a v \frac{m N_A}{MW} \quad (2.4)$$

where, $\,\alpha$ the abundance of the mother nucleus in the natural composition

v, the number of atoms of the nucleus of interest in the molecular used as target material w, the same labeled mass

m, the sample's mass

 $N_{A,}$ the Avogadro number

MW, the molecular weight of nuclei contained into the sample (the sample may contain different elements)

It has to be mentioned that it is important that the sample radius is smaller than the beam radius as to be fully irradiated from the neutron beam. Otherwise in the calculation the sample mass corresponding to the beam profile has to be taken into account.

Considering the flux Φ , in most of the neutron physics experiments it cannot be measured directly. In such cases, flux is calculated using reference foils. These foils are placed front and back of the main sample ("sandwich technique"), so as to be irradiated by the beam as well. The induced reactions must lead to the formation of daughter nuclei with adequate half-life times and have a well known cross section. If these requirements and the rest mentioned above are fulfilled, the flux can be calculated as the inverse solution of the equation (2.1) mentioned at the begin of this chapter:

$$\Phi = \frac{A C F_{SA} C F_{DT}}{N_T \sigma \varepsilon I_{\gamma} (1 - e^{-\lambda t_m}) e^{-\lambda t_w} f_b} \quad (2.5)$$

2.2 Erbium target and reference foils

The ¹⁶³Er* compound nucleus produced after the interaction between the ¹⁶²Er and the neutron is decayed by the emissions of two neutrons. The ¹⁶¹Er nucleus formated in the sample is unstable with half-life time $T_{1/2}$ =3.21 h and it is decayed by 100% electron capture towards to ¹⁶¹Ho. The ¹⁶¹Ho decays to the ground state through γ -ray emissions. Because of the large number of γ -rays the ¹⁶¹Er decay scheme is complicated enough. Among of the γ -rays emitted the stronger one and the one used within the present work is at E_{γ} =826.6 keV with intensity I=64% (4) [15]. The neutron flux was estimated by the following reference reactions:

- ${}^{27}\text{Al}(n,a){}^{24}\text{Na}$, Q=-3.132 MeV
- 197 Au(n,2n) 196 Au, Q=-8.072 MeV
- ${}^{93}Nb(n,2n){}^{92m}Nb$, Q=-8.830 MeV

The decays of the unstable nuclei produced are described by the following decay-schemes:

• <u>²⁴Na daughter nucleus</u>



Figure 2.1: decay scheme of ²⁴Na unstable nucleus

• ¹⁹⁶Au daughter nucleus



Figure 2.2: decay scheme of ¹⁹⁶Au unstable nucleus

• ^{92m}Nb daughter nucleus



Figure 2.3: decay scheme of the ^{92m}Nb unstable nucleus

The γ -rays by which the reference foils activity was determined are mentioned in the table (2.1) ([16]-[18]):

reference foils	daughter nuclei	T _{1/2}	E _γ (keV)	I (%)	σ ₁ (%)
²⁷ AI	²⁴ Na	14.997 h	1368.626	99.9936	0.0015
¹⁹⁷ Au	¹⁹⁶ Au	6.1669 d	333.03	22.881	0.946
⁹³ Nb	^{92m} Nb	10.15 d	934.44	99.15	-

Table 2.1: γ-rays emitted during the reference foils' daughter nuclei decay

2.3 Neutron beam

The neutron beams are always secondary beams produced by a variety of nuclear reactions depending on the primary beam characteristics, the neutron beam energy and the specific experimental conditions.

Within the present work the adopted reaction for the production of the quasi-mono-energetic neutron beams was:

$$^{2}_{1}H + ^{2}_{1}H \rightarrow n + ^{3}_{2}H$$

widely known as the D-D reaction. D-D is an exothermic reaction with Q-value=3.26 MeV

The deuterium beams were provided by the 5.5 MV Tandem Van der Graaf accelerator of the Institute of Nuclear and Particle Physics at N.C.S.R "Demokritos". The deuterium beam was directed and focused to a deuterium gas target. During the irradiations the gas target pressure was 1250 mbar. The gas pressure in the gas-shell was remotely controlled and was kept constant by means of a micro-metric vane.

Three irradiations were conducted at neutron energies of 10.7 MeV, 11.0 MeV and 11.3 MeV. The correspondence of the neutron beam energy with the deuterium beam energy is given on the Table 2.2.

E _d (MeV)	E _n (MeV)	
7.86	10.7	
8.17	11.0	
8.47 11.3		
Table 2.2: the deuterium bombarding		
energies and the respective neutron		
energies produced		

A simulation of the energy distribution of the neutrons produced for each deuterium irradiation was produced via the NeuSDesc code [19], which confirmed the values of the neutron beams energies:



• for E_d=7.86 MeV

Figure 2.4: neutron energy distribution for bombarding deuterium energy E_d =7.86 MeV

• for E_d =8.17 MeV,



 $\underline{Figure~2.5}:$ neutron energy distribution for bombarding deuterium energy $E_d{=}8.17~MeV$

• for E_d =8.47 MeV



<u>Figure 2.6</u>: neutron energy distribution for bombarding deuterium energy E_d =8.47 MeV

2.4 Neutron beam fluctuations and BF_3 Detector

In order to take into account in an accurate way the decay of the product nuclei during the irradiation the neuron beam intensity-fluctuations have to be recorded by means of a Multi-Channel-Scaller. For this reason a BF_3 detector was used as neutron counter.

BF₃ detector's function:

The BF_3 detector is as a proportional counter, which is filled with BF_3 gas, usually enriched to more than 90 percent in ¹⁰B. The neutron detection is based on the following reaction :

$${}^{10}B+n \rightarrow {}^{4}He + {}^{7}Li$$

The above reaction is an exothermic reaction and concerning whether the 7 Li is formed in the ground or in an excited state it has different Q-values:

- ⁷Li at ground state: Q-value=2.792 MeV
- ⁷Li at excited state: Q-value=2.31 MeV (0.480 MeV is converted into ⁷Li excitation energy → less energy is emitted)

In the 94 % of the reactions the ⁷Li is left in an excited state, whereas the rest 6 % of them leave ⁷Li in the ground state.

The alpha and ⁷Li particles produced are emitted at opposite directions (linear momentum conservation).



<u>Figure 2.7</u>: the alpha and ⁷Li particles produced at the BF₃ detectors travel off at opposite directions

During their transportation inside the gas, the alpha and ⁷Li particles ionize the gas and create primary ion pairs. The electrons from the primary ion pairs create further "secondary" ion pairs as they get close to the anode (avalanche electrons).

The electrons are approaching the anode and the positive charged ions are moving towards the cathode. In this way, pulses are created. Their size depends on whether the ⁷Li is formed at the ground or at the excited state. In the first case, the alpha and ⁷Li particle have more kinetic energy and ,consequently, a higher pulse results. Respectively, the pulse has a smaller height when ⁷Li is excited.

The ${}^{10}B(n,\alpha)^7$ Li reaction cross section has an energy dependence equal to $1/\sqrt{E_n}$. For this reason, BF₃ counters, almost exclusively, respond to thermal neutrons, whereas the cross section for the absorption of fast neutrons by ${}^{10}B$ is much smaller. Therefore, as to increase the intrinsic detection efficiency the incident neutrons are moderated. For this reason the BF₃ gas counter is placed inside a paraffin moderator in barrel configuration. For the same reason any information for the initial kinetic energy of the neutrons finally lost thought the moderation process.

Neutron flux fluctuations recorded by the BF₃ counter

During the irradiations the neutron flux was recorded by means of a Multi-Channel- Scaler. Every 60 sec the total number of pulses were recorded.

• Neutron Irradiation Energy: 10.7 MeV



Figure 2.8: neutron fluctuations as recorded from the BF_3 counter for E_n =10.7 MeV

• Neutron Irradiation Energy 11.0 MeV



Figure 2.9: neutron fluctuations as recorded from the BF₃ counter for E_n=11.0 MeV



2.5 Irradiation Set-up

For the estimation of flux, reference foils of 27 Al, 197 Au and 93 Nb were used. They were placed front and back of the erbium pellet ("sandwich technique") at a distance of 5 cm from the D₂ gas target :



<u>Figure 2.11</u>: schematic representation of the reference foils and the erbium pellet place



Figure 2.12: irradiation set-up



Figure 2.13: irradiation set-up

Each irradiation last about 10 h (~3 $T_{1/2}$, 3 times the half-life time of 161 Er).

	E _n (MeV)	Irradiation time (s)
first irradiation	10.7	35820
second irradiation	11.0	35580
third irradiation	11.3	36360

<u> Table 2.3</u> :	irradiation	times

In the irradiations two erbium targets were used:

	mass (mgr)	diameter (mm)	thickness (mm)
erbium target A	994.43	12.95	2.00
erbium target B	1059.65	12.95	1.99

Table 2.4: mass and geometrical characteristics of the erbium targets

2.6 γ -ray Detectors

After the irradiations, the induced activity of the erbium sample and the reference foils was measured using two100% relative efficiency HPGe and one 16% relative efficiency HPGe detectors.

Because of the minimal abundance of $^{162}{\rm Er}$ in natural sample composition (0.139%) the maximum possible efficiency was necessary. For this reason, the $^{161}{\rm Er}$ decay detection was carried out by the two HPGe detectors with 100% relative efficiency. They were placed in close geometry in a distance of some centimeters, whereas the erbium pellet was at the middle of this distance. In this way a solid angle ${\sim}4\pi$ was covered.



Figure 2.14: the 2x100% HPGe detectors used for the erbium pellet activity measurement

By measuring the γ -ray activity at close geometry the detection solid angle is increased and therefore the detection efficiency is also enhanced. On the other hand the issue of summing effects arises when a close detection geometry is adopted. For this reason the calibration of the detector was done by using a ⁵⁴Mn point source where a single γ -ray line at 835 keV- very close to the 827 keV decay line of ¹⁶¹Er is emitted (see also next paragraph). Furthermore, despite the complexity of the ¹⁶¹Er decay scheme the 827 keV line is emitted with multiplicity 1-(within ~1% approximation).

The reference foils' activity measurements were conducted by the 16% HPGe detector. The distance from the detector's window was at 7 cm. In this way it was ensured that the measurement was free from coincidence-summing effects. Because of the small half-life time of ²⁴Na ($T_{1/2}$ =14.997 h), it was necessary the aluminum foils to be placed first at the detector and afterwards the rest.



Figure 2.15: the 16% HPGe detector used for the measurement of the foils activity

The three detectors were adjusted to operate simultaneously. Every hour the recorded spectra were saved and erased. In this way possible data loss was avoided and secondly the decay rate of the measured activity could be followed.

2.7 Detectors calibration

 $^{161}\mathrm{Er}$ decays through EC (100%) by feeding several excited states of the daughter nucleus $^{161}\mathrm{Ho}$ resulting in a quite complicated decay scheme:



Figure 2.16: Decay Scheme of ¹⁶¹Er

The ^{161}Ho nucleus decays to its ground state through the emission of several γ -rays , but the strongest one is 826.6 keV. For the calibration of the 2x100% HPGe detectors at this energy, a point ^{54}Mn source was placed between the 2x100% HPGe detectors at the same distance as the erbium pellet.

The ⁵⁴Mn is one of the unstable isotopes of Mn nuclei with half-life time $T_{1/2}$ = 312.20 days. During its decay, it emits γ -rays of 834.8 keV energy with an intensity equal to 99.9760 % (10) [20]. The point source of ⁵⁴Mn was adopted for the calibration of the two 100 % HPGe detectors for two reasons: Firstly, the energy of the emitted photon is very close to the region of interest for the ¹⁶¹Er decay (827 keV) and secondly is a mono-energetic γ -ray source. The fact that the γ -ray multiplicity is equal to one, as can be seen in Fig. 1.16, is important because corrections for coincidence summing effects are not needed.



Figure 2.17: ⁵⁴Mn decay scheme

The 16% HPGe detector was calibrated in an extended energy range as to cover the detection needs for the used reference foils. For this purpose, a point source of ¹⁵²Eu was placed at distances of 7 cm and 13 cm from the detector's window. ¹⁵²Eu is one of the unstable isotopes of Eu with half-life time $T_{1/2}$ = 13.517 years. It appears a quite complicated decay scheme, as is decayed by the emission of many strong γ -rays from some hundreds keV up to ~1400 keV [21].

3. Data Analysis

3.1 Calibration curves of 16% HPGe Detector

For the calibration curves of the 16% HPGe detector a point source of 152 Eu was placed at 7 cm and at 13 cm distance from the detector's window. This source emits photons at different energies. The characteristics photon energies, the intensities and the corresponding uncertainties of 152 Eu are summarized in the Table 3.1 :

Eγ (keV)	I (%)	σ _, (%)
244.6974	7.55	0.04
344.2785	26.59	0.21
443.9606	2.827	0.015
778.9045	12.93	0.09
964.057	14.51	0.07
1112.076	13.67	0.09
1408.013	20.87	0.10

<u>Table 3.1</u>: ¹⁵²Eu decay energies and the respective intensities

A characteristic spectrum of $^{\rm 152}{\rm Eu}$ decay is:



A detector's efficiency is equal to the ratio of the counts detected to the total source's emissions at the detector's Data Acquisition Time (DAQ-time):

$$\varepsilon = \frac{counts}{emissions}$$
 (eq. 3.1)

The photons emitted by the point source during DAQ-time are calculated via the equation:

$$emissions = A I DAQ - time$$
 (3.2)

where A is the source's activity

The ^{152}Eu point source had known activity: $A_0\text{=}(217\pm3)\,$ kBq at 01/01/2011. So the date of the experiment conduction at 12/02/2014 had activity equal to A=(185 ± 3) kBq , concerning the decay law:

$$A = A_o e^{-\lambda t} \quad (3.3)$$

where the decay constant $\lambda = (0.05128 \pm 0.00005)$ 1/years
t= 1138 days

In the following table the total counts', emissions' and efficiencies' results are presented with the respective errors :

• for 7 cm source-detector's window distance. The DAQ-time was considered equal to detector's live-time=2250.797 s (the part of the DAQ-time for which the detector's electronics were active). The DAQ dead-time correction factor was equal to 1.

Eγ (keV)	counts	σ_{counts}	emissions	$\sigma_{_{emissions}}$	efficiency	$\sigma_{_{efficiency}}$
244.6974	270128	697	31427363	465320	0.00860	0.00013
344.2785	676152	912	110682595	1742081	0.00611	0.00010
443.9606	58603	365	11767570	172819	0.00498	0.00008
778.9045	140796	451	53821961	815249	0.00262	0.00004
964.057	127984	418	60398814	884442	0.00212	0.00003
1112.076	106691	386	56902259	854299	0.00187	0.00003
1408.013	129429	367	86872725	1258161	0.00149	0.00002

Table 3.2: 16% HPGe detector efficiencies for ¹⁵²Eu decay energies at 7 cm



34

E _γ (keV)	counts	$\sigma_{_{counts}}$	emissions	$\sigma_{_{emissions}}$	efficiency	$\sigma_{_{efficiency}}$
244.6974	211070	603	61842244	915649	0.00341	0.00005
344.2785	520819	797	217799374	3428038	0.00239	0.00004
443.9606	46510	315	23156030	340070	0.00201	0.00003
778.9045	111061	393	105909963	1604233	0.00105	0.00002
964.057	102680	366	118851783	1740391	0.00086	0.00001
1112.076	84335.6	327	111971322	1681075	0.00075	0.00001
1408.013	103327	325	170946707	2475788	0.00060	0.00009

• for 13 cm source-detector's window distance and detector's live-time=4429.081 s

Table 3.3: 16% HPGe detector efficiencies for ¹⁵²Eu decay energies at 13 cm



3.2 Reference foils' efficiency

The 16% HPGe detector's efficiencies at reference foils decay energies at 7 cm were determined using the ln(efficiency)= $f(lnE_{\gamma})$ graph (Fig. 3.4), which follows linear trend. For the error determination the 68% confidence level bands were designed in the same graph. The bands depict the upper and lower confidence bounds of all the points on the fitted line withing the range of data, and as a result the upper and the lower values of the respective efficiencies.



<u>Figure 3.4</u>: ln(efficiency)=**f**(lnE γ) graph for the 16% HPGe Detector at 7 cm.

From the above graph the following results accrued:

reference foils	daughter nuclei	decay energy (keV)	efficiency	$\sigma_{_{efficiency}}$
²⁷ AI	²⁴ Na	1368.626	0.00151	0.00003
¹⁹⁷ Au	¹⁹⁶ Au	333.03	0.00636	0.0001
⁹³ Nb	^{92m} Nb	934.44	0.00223	0.00003

Table 3.4: 16% HPGe detector efficiency for the reference foils' decay energies at 7 cm
3.3 2x100 % HPGe Detectors efficiency

⁵⁴Mn Activity determination

As mentioned previously the 2x100% HPGe detectors were calibrated only for the ⁵⁴Mn decay energy at 834.8 keV. The problem with the ⁵⁴Mn point source was its unknown activity. To overcome this problem ⁵⁴Mn was placed at except for the 2x100% HPGe detectors at the 16 % HPGe detector as well, at the distance of 13 cm from the detector's window.



The efficiency of the 16 % HPGe detector at 834.8 keV at 13 cm distance from the detector's window was calculated from the graph $\ln(\text{efficiency})=\mathbf{f}((\ln E\gamma))$ (Fig. 3.6) and was found equal to:

 $efficiency = (0.00100 \pm 0.00001)$



<u>Figure 3.6</u>: $\ln(\text{efficiency})=f(\ln E\gamma)$ graph for the 16% HPGe Detector at 13 cm

Since the efficiency and the counts of this decay energy were known, the respective emissions and , consequently, the ^{54}Mn source's activity could be determined via the equations $\,:\,$

$$emissions = \frac{counts}{efficiency}$$
 (eq 3.4) & $Activity = \frac{emissions}{I \ live \ time}$ (eq.3.5)

• for detector's live-time=3599.682 s

Ey (keV)	efficiency	$\sigma_{_{efficiency}}$	counts	σ_{counts}	emissions	$\sigma_{_{emissions}}$	A (Bq)	σ _^ (Bq)
834.848	0.00100	0.00001	1912	44	1907451	51647	530	14

Table 3.5: Mn-54 Activity determination

Finally,
$$A = (530 \pm 14) Bq$$

$\frac{54}{Mn}$ efficiency determination

After calculating the activity, the 54 Mn efficiency was calculated for each of the two 100% HPGe detectors separately, but also, for both of them by adding the separate spectra:

• first detector, $live time_1 = 4478.233 s$:

Ey (keV)	counts	σ_{counts}	emissions	$\sigma_{_{emissions}}$	efficiency	$\sigma_{_{efficiency}}$
834.848	134012	368	2372990	64253	0.056	0.002

Table 3.6: efficiency determination of the first 100% HPGe detector at 834.848 keV energy at close geometry

• second detector, $live time_2 = 4480.267 s$:

Ey (keV)	counts	σ_{counts}	emissions	$\sigma_{_{emissions}}$	efficiency	$\sigma_{_{efficiency}}$
834.848	117832	345	2374068	64282	0.050	0.001
						•

Table 3.7: efficiency determination of the second 100% HPGe detector at 834.848 keV energy at close geometry

• both detectors,
$$live time = \frac{live time_1 + live time_2}{2} = 4479.25 s$$
:

Ey (keV)	counts	σ_{counts}	emissions	$\sigma_{emissions}$	efficiency	$\sigma_{_{efficiency}}$
834.848	252690	505	2373529	64268	0.106	0.003

Table 3.8: total efficiency for the 2x100% HPGe detectors at 834.848 keV energy at close geometry

3.4 Activity Measurements

3.4.1 Reference foils activity measurements

For the determination of the neutrons flux three reference reactions were used: $^{27}Al(n,a)^{24}Na$, $^{197}Au(n,2n)^{196}Au$ and $^{93}Nb(n,2n)^{92m}Nb$.

The information about details of the γ -ray activity measurements are given in this paragraph. Below some explanation with respect the used terminology is also given.

- live-time : the part of Data Acquisition Time (DAQ-Time) for which the detector electronics were active
- real-time: the actual DAQ-Time
- dead-time: the total time interval that DAQ system is busy for recording the detected pulses (real time-live time)
- waiting time: the time interval between the beam stop and the starting of $\gamma\text{-ray}$ activity measurement

The final spectra were generated by adding the individual 1 hour spectra, which were recorded by the 16% HPGe detector. Respectively, the final real-times and live-times are the sum of the real-time and live-time of the added spectra.

Moreover, the graphs counts= \mathbf{f} (real time) are presented. The graphs were fitted by the equation:

 $counts = A[0](1 - e^{(-\lambda * realtime)})$ (eq. 3.6)

where λ , the decay constant of the daughter nuclei

$$A[0] = efficiency I N_{act} e^{(-\lambda * waiting time)}$$
 (eq. 3.7)

(Nact: the number of unstable nuclei at the stop of irradiation)

• first irradiation: $E_n = 10.7 \text{ MeV} \rightarrow {}^{27}\text{Al}(n,a)^{24}\text{Na}$ reference reaction



Figure 3.7: ²⁴Na spectrum at 16% HPGe Detector at 7 cm distance from the detector's window

• front Al-foil

measuring time (s)	28813			
waiting time (s)	16967			
Table 3.9: measuring and waiting time for the				

Al front foil

spectra	real-time (s)	live-time (s)	counts	σ _{counts}	counts relative error
1 st	3600	3599.824	243	16	0.07
2 nd	7200	7199.623	490	23	0.05
3 rd	10800	10799.403	718	28	0.04
4 th	14400	14399.231	941	32	0.03
5 th	18000	17999.004	1137	36	0.03
6 th	21600	21598.78	1329	39	0.03
7 th	25200	25198.584	1529	43	0.03
8 th	28800	28798.393	1700	45	0.03

Table 3.10: the 16% HPGe detector real-times and live-times and the counts detected for the Al front foil



<u>Figure 3.8:</u> the counts= \mathbf{f} (real time) graph for the Al front foil. The red line corresponds to the expected growth of counts considering the half-life time of ²⁴Na

fitting parameter: $A[0] = (5517 \pm 66)$

• back Al-foil

measuring time (s)	14406
waiting time (s)	1961

Table 3.11 measuring and waiting time for the Al back foil

spectra	real-time (s)	live-time (s)	counts	$\sigma_{_{counts}}$	counts relative error
1 st	3600	3599.75	304	19	0.06
2 nd	7200	7199.53	561	25	0.04
3 rd	10800	10799.334	794	30	0.04
4 th	14400	14399.123	1009	34	0.03

Table 3.12: 16% HPGe detector real-times and live-times and the counts detected for the Al back foil



<u>Figure 3.9</u>: the counts=**f**(real time) graph for the Al back foil. The red line corresponds to the expected growth of counts considering the half-life time of ²⁴Na

fitting parameter: $A[0]=6170\pm128$

• second irradiation: $E_n=11.0 \text{ MeV} \rightarrow {}^{97}\text{Au}(n,2n)^{196}\text{Au}$



Figure 3.10: Part of the ¹⁹⁶Au spectrum at 16% HPGe Detector at 7 cm distance from the detector's window. The characteristic decay-line at 333.03 keV can be seen.

• front Au-foil

601
6450

Table 3.13: measuring and waiting time for the

Au front foil

spectra	real-time (s)	live-time (s)	counts	σ_{counts}	counts relative error
1 st	3600	3599.454	2609	56	0.02

Table 3.14: 16% HPGe detector real-times and live-times and the counts detected for the Au front foil

• back Au-foil

measuring time (s)	14406
waiting time (s)	121311

Table 3.15: measuring and waiting time for the Au back foil

spectra	real time (s)	live time (s)	counts	σ_{counts}	counts relative error
1 st	3600	3599.509	2335	52	0.02
2 nd	7200	7198.984	4571	75	0.02
3 rd	10800	10798.475	6828	91	0.01
4 th	14400	14397.984	9060	104	0.01

Table 3.16: 16% HPGe detector real-times and live-times and the counts detected for the Au back foil



<u>Figure 3.11</u>: the counts=**f**(real time) graph for the Au back foil. The red line corresponds to the expected growth of counts considering the half-life time of ¹⁹⁶Au.

fitting parameter: A[0]= (490149 ± 3561)

third irradiation: En=11.3 MeV \rightarrow ⁹³Nb(n,2n)^{92m}Nb



Figure 3.12: 92mNb spectrum at 16% HPGe Detector at 7 cm distance from the detector's window

• front Nb-foil

measuring time (s)	18007
waiting time (s)	21293

<u>Table 3.17</u>: measuring and waiting time for the Nb front foil

spectra	real-time (s)	live-time (s)	counts	$\sigma_{_{counts}}$	counts relative error
1 st	3600	3599.744	46	11	0.24
2 nd	7200	7199.506	84	16	0.19
3 rd	10800	10799.297	127	21	0.17
4 th	14400	14399.064	180	27	0.15
5 th	18000	17998.831	207	25	0.12

 Table 3.18:
 the 16% HPGe detector real-times and live-times and the counts detected for the Nb front foil. The red line corresponds to the expected growth of counts considering the half-life time of ^{92m}Nb



fitting parameter: $A[0]=(15117\pm1084)$

• back Nb-foil

measuring time (s)	18439
waiting time (s)	2286
TT 1 D 40	

Table 3.19: measuring and waiting time for the Nb back foil

spectra	real time (s)	live time (s)	counts	σ_{counts}	counts relative error
1 st	3960.759	3960.462	54	11	0.20
2 nd	7560.759	7560.209	93	15	0.16
3 rd	11160.759	11159.984	144	18	0.13
4 th	14760.759	14759.773	176	21	0.12
5 th	1830.759	18359.563	211	25	0.12

Table 3.20: the 16% HPGe detector real-times and live-times and the counts detected for the Nb back foil



 $\label{eq:Figure 3.14: the counts} \ensuremath{=}\ensuremath{\,f}\xspace(real time) \ensuremath{\,graph}\xspace for the Nb back foil. The red line corresponds to the expected growth of counts considering the half-life time of $$^{92m}\Nb$.}$

fitting parameter: $A[0]=(15499\pm948)$

3.4.2 ¹⁶¹Er Activity

The decay rate of ¹⁶¹Er was recorded following the counting rate of the most intense decay transition at 826.6 keV. The region of interest of the erbium sample γ -ray spectrum after 10 h of irradiation at 11.0 MeV neutron beam is presented at Figure 3.15. This spectrum resulted after 10 h of data acquisition. For the counts measurement the spectra of each 100% HPGe detector were added. For this reason before the measurement both detectors were very carefully gain matched.



¹⁶¹Er decay

Below the information about the recorded counts measuring time, the waiting time of measurement after the end of the irradiation and the counts measured are presented. Moreover the detectors' live-time and real-time are mentioned.

• first irradiation: E_n=10.7 MeV

measuring time (s)	14406			
waiting time (s)	1961			
Table 3.21: measuring and waiting time for				
the erbium target				

spectra	real-time (s)	live-time (s)	counts	$\sigma_{_{counts}}$	counts relative error
1 st	3600	3597.245	144	29	0.20
2 nd	7200	7194.4725	199	34	0.17
3 rd	10800	10791.9495	289	46	0.16
4 th	14400	13389.3745	324	52	0.16

Table 3.22: the 2x100% HPGe detectors real times and live times and the counts detected for the erbium target



<u>Figure 3.16</u>: the counts=f(real time) graph for the erbium target. The red line corresponds to the expected growth of counts considering the half-life time of 161 Er.

fitting parameter: $A[0]=(596\pm51)$

- second irradiation: E_n =11.0 MeV

measuring time (s)	36378	
waiting time (s)	1894	
Table 2.22, measuring and waiting time for the		

<u>Table 3.23:</u> measuring and waiting time for the erbium target

spectra	real-time (s)	live-time (s)	counts	σ_{counts}	counts relative error
1 st	3600	3596.767	776	39	0.05
2 nd	7200	7193.7445	1486	56	0.04
3 rd	10800	10790.7935	1987	67	0.03
4 th	14400	14387.892	2445	75	0.03
5 th	18000	17985.068	2761	84	0.03
6 th	21600	21582.2845	3113	91	0.03
7 th	25200	25179.572	3295	98	0.03
8 th	28800	28776.9005	3525	104	0.03
9 th	32400	32374.28	3738	109	0.03
10 th	36000	35971.67	3871	113	0.03

Table 3.24: the 2x100% HPGe detectors real-times and live-times and the counts detected for the erbium target



<u>Table 3.17</u>: the counts=f(real time) graph for the erbium target. The red line corresponds to the expected growth of counts considering the half-life time of ¹⁶¹Er.

fitting parameter: $A[0]=(4252\pm43)$

• third irradiation: En=11.3 MeV

measuring time (s)	18439
waiting time (s)	2286

Table 3.25: measuring and waiting time for the erbium target

spectra	real-time (s)	live-time (s)	counts	σ_{counts}	counts relative error
1 st	3960.759	3957.7745	271	35	0.13
2 nd	7560.759	7555.25	306	39	0.13
3 rd	11160.759	11152.764	405	47	0.12
4 th	14760.759	14750.263	513	54	0.11
5 th	18360.759	18347.734	574	60	0.10

Table 3.26: the 2x100% HPGe detectors real-times and live-times and the counts detected for the erbium target



<u>Figure 3.18</u>: Table 18: the counts=f(real time) graph for the erbium target. The red line corresponds to the expected growth of counts considering the half-life time of ¹⁶¹Er.

fitting parameter: $A[0] = (885 \pm 46)$

3.5 Correction factors

3.5.1 Decay during irradiation correction factor

During the irradiations of the erbium sample unstable nuclei N_{act} (activated nuclei) were produced. Their rate of change is given from the equation:

$$\frac{dN_{act}}{dt} = \sigma f(t) N_T - \lambda N_{act} \quad (eq. 3.9)$$

where the first term describes the production of the activated nuclei and the second one their simultaneous decay.

The solution of the above differential equation is:

$$N_{act} = \sigma \Phi N_T f_b$$
 (eq. 3.10)

where
$$f_b = \frac{\int_{0}^{t_{ir}} f(t)e^{\lambda t}dt}{\int_{0}^{t_{ir}} f(t)dt} e^{-\lambda t_{ir}}$$
 (eq. 3.11)

calculates the balance between the activated nuclei that formed and them that decayed during the irradiation

Depending on whether the irradiation flux was constant or non-constant the $f_{\rm b}$ correction factor has two different solutions:

• for constant flux: $f(t) \rightarrow f_0$, the above equation has a simple analytical solution

$$f_{b} = \frac{(1 - e^{-\lambda t_{ir}})}{\lambda t_{ir}}$$
 (eq. 3.12)

- for non-constant neutron flux the correction factor f_b becomes:

$$f_{b} = \frac{e^{-\lambda t_{w}} \sum_{i=1} f_{i} (e^{(i+1)\lambda dt} - e^{i\lambda dt})}{\lambda dt \sum_{i=1} f_{i}} \quad (eq. \ 3.13)$$

Since the neutron flux was non-constant for the three irradiations at 10.7 MeV, 11.0 MeV and 11.3 MeV, a program has been developed at C++ programming language (see appendix B), which calculates the f_b correction factor in accordance with the above equation by taking into account the recorded neutron flux history files.

The f_b values for the erbium target and the reference foils are referred for each irradiation in the Table (3.27) :

first irradiation, E _n =10.7 MeV				
targets	f _b			
¹⁶² Er	0.386853			
²⁷ AI	0.791465			
second irradiation, E _n =11.0 MeV				
targets	f _b			
¹⁶² Er	0.404055			
¹⁹⁷ Au	0.97669			
third irradia	third irradiation, E _n =11.3 MeV			
targets	f _b			
¹⁶² Er	0.415989			
⁹³ Nb	0.985985			

Table 3.27: $f_{\scriptscriptstyle b}$ results as calculated for non-constant flux

The two correction factors referred below correct the fact that the counts detected are fewer than these the detectors should detect concerning their efficiency:

3.5.2 Self-Attenuation Correction factor

After the irradiation the number of activated nuclei is determined from the counting rate of the emitted γ -rays. A certain percentage of the emitted γ -rays is attenuated from the sample material and this has to be taken into account. For this reason the self-attenuation CF_{SA} correction factor has to be estimated.

total counts =
$$CF_{SA}$$
 * detected counts $\Rightarrow CF_{SA} = \frac{\text{total counts}}{\text{detected counts}}$ (eq. 3.14)

where the total counts are the counts that would be detected supposing that there is no selfattenuation, i.e. the counts that would be detected in case the targets were point massless sources of γ radiation.

In equivalence, the self-attenuation correction factor CF_{SA} can be expressed as the ratio of the detector's efficiency when the targets are point massless sources (ideal case) to the detector's efficiency when the targets are extended sources (actual case):

$$CF_{SA} = \frac{efficiency_{PS}}{efficiency_{ES}}$$
 (eq. 3.15)

where efficiency $_{\rm PS}$, the efficiency for point source $efficiency_{\rm ES},$ the efficiency for extended source

For the numerical determination of the terms $efficiency_{FS}$ and $efficiency_{ES}$ extended Geant4 Monte Carlo simulations were performed (see Appendix C). Firstly, the Geant4 MC simulations were tested by adopting the detector manufacturer geometrical specifications. The experimentally deduced detection efficiency was reproduced for several source to detector distances. Afterwards, the actual detection

geometry during the sample measurements was implemented in the Geant4 MC calculations for point source (PS) and for the extended source (ES).

source	E _γ (keV)	thickness (mm)	CF _{SA}	$\sigma_{_{CF}}$
²⁴ Na	1368.626	0.50	1.005	0.005
¹⁹⁶ Au	333.03	0.50	1.128	0.002
^{92m} Nb	934.44	0.40	1.007	0.004

<u>Table 3.28</u>: the self-attenuation correction factors for the reference foils decay energies as estimated with the Geant4 MC calculations.

In the case of the erbium target the role of the CF_{SA} was dual: it does not only correct for the selfattenuation but also corrects for the fact that the 2x100% HPGe detectors were calibrated at 834.8 keV (⁵⁴Mn decay energy) and not at 826.6 keV which is the energy of the photons emitted during ¹⁶¹Er decay:

So for the erbium target: $CF_{SA} = \frac{efficiency_{54}}{efficiency_{161}}$ (eq. 3.16)

where $efficiency_{54Mn}$ and $efficiency_{161Er}$ are the Geant4 code efficiency results for the ⁵⁴Mn point source and the erbium target (considering the real dimensions) respectively.

source	E _γ (keV)	thickness (mm)	CF_{SA}	$\sigma_{_{\sf CF}}$
¹⁶¹ Er	826.6	2	1.023	0.005

Table 3.29: the self- attenuation correction factor for the erbium target as estimated with the Geant4 MC calculations.

3.5.3 Dead-Time Correction factor

When a signal is recorded for a certain period of time the DAQ system is inactive. This time period corresponds to the needed time for signal processing and recording. This period of time (dead-time) for the total number of counts has to be taken into account. In this way the duration of measurement (real-time) is slightly different from the total time where the detector is actually active (live-time).

$$CF_{DT} = \frac{realtime}{livetime}$$
 (eq. 3.17)

3.6 Reference reactions cross sections

En	(MeV)	reference reaction	cross section (barns)	$\sigma_{\rm crosssection}$ (barns)
10.7	²⁷ Al(n,α) ²⁴ Nα	0.102	0.001	
	¹⁹⁷ Au(n,2n) ¹⁹⁶ Au	1.35	0.04	
		⁹³ Nb(n,2n) ^{92m} Nb	0.244	0.003
		²⁷ Al(n,α) ²⁴ Nα	0.106	0.001
11.0	¹⁹⁷ Au(n,2n) ¹⁹⁶ Au	1.45	0.04	
	⁹³ Nb(n,2n) ^{92m} Nb	0.285	0.004	
11.3	²⁷ Al(n,α) ²⁴ Nα	0.109	0.001	
	¹⁹⁷ Au(n,2n) ¹⁹⁶ Au	1.55	0.04	
	⁹³ Nb(n,2n) ^{92m} Nb	0.322	0.004	

The reference reactions cross sections were retrieved from the IRDFF data base [22]. In accordance to this:

Table 3.30: the reference reactions cross section as retrieved from the IRDF v.1.05 data base.

3.7 Neutron Flux

The neutron flux during the erbium target irradiations was obtained from the mean value of the recorded neutron flux using the afore mentioned reference reactions. The monitor foils were placed front and back with respect the erbium target. The neutron flux uncertainty is 7% of the mean value:

$$\Phi = \frac{\Phi_{front} + \Phi_{back}}{2}$$
 (eq. 3.18) & $\sigma_{\phi} = 0.07 \Phi$ (eq. 3.19)

irradiation	foil	Φ (neutrons/cm ²)
En-10 7 Mo\/	foil-front	1.37E+10
EII-10.7 MeV	foil-back	1.21E+10
$E_{n-11} 0 M_{0}$	foil-front	7.89E+10
EII-II.0 Mev	foil-back	7.11E+10
$E_{n-11} = M_{0}/$	foil-front	1.10E+10
foil-back		1.07E+10

Table 3.31: the neutrons fluxes at the front and back foils of the erbium target

The results of the integrated neutron flux at the erbium target are summarized in the Table 3.32:

E _n (MeV)	Φ (neutron/cm ²)	σ_{ϕ} (neutron/cm ²)
10.7	1.29E+10	0.09E+10
11.0	7.50E+10	0.53E+10
11.3	1.09E+10	0.08E+10

<u>Table 3.32</u>: results for the integrated neutron flux at the erbium target

4. Results

As described previously the neutron flux was determined by recording the induced activity of the monitor foils according to the reference reactions. In this way all the parameters are known and the eq. 2.1 given below can be used as to deduce the reaction cross section:

$$\sigma = \frac{A CF_{SA} CF_{DT}}{N_T \Phi \varepsilon I_v (1 - e^{-\lambda t_m}) e^{-\lambda t_w} f_b}$$

The ${}^{162}\text{Er}(n,2n){}^{161}\text{Er}$ reaction cross section at neutron energies of 10.7 MeV, 11.0 MeV and 11.3 MeV can be finally measured. The results are summarized in the Table 3.33. The graphical representation of the reaction cross section experimental results from the present work along with previous experimental results are presented in Fig. 3.19.

E _n (MeV)	cross section (barns)	$\sigma_{_{crosssection}}$ (barns)
10.7	0.44	0.08
11.0	0.56	0.06
11.3	0.71	0.10

Table 3.33: final cross section results



Figure 3.19: cross section graph for the ¹⁶²Er(n,2n)¹⁶¹Er compound nucleus interaction

5. Conclusions

The ¹⁶²Er(n,2n)¹⁶¹Er reaction cross section was measured for the first time at near threshold energies, at 10.7 MeV, 11.0 MeV and 11.3 MeV. The high sensitivity and the analytical power of the Activation Technique was important given that the abundance of ¹⁶²Er in the natural composition Erbium sample is only 0.139%. The minimal abundance of ¹⁶²Er in the sample was compensated by using an efficient 4π γ -ray detection set-up consisting of two 100 % relative efficiency HPGe detectors in close geometry. In future, the results of the present work along with the existing experimental data can be combined as to improve the "local" parameterization of the compound nucleus theoretical calculations. Furthermore, experimental data at higher neutron beam energies (e.g. E_n >17 MeV) are also needed as to map the excitation function.

Appendix A

The Cross Section equation

The formula which gives the cross section value in Activation Technique:

$$\sigma = \frac{counts}{\Phi I \varepsilon N_T e^{-\lambda t_w} (1 - e^{-\lambda t_m}) f_b}$$

is proven by combining the solution of the equation which describes the production of the unstable nuclei $N_{\rm act}$ with the solution of the equation which describes their decay.

<u>N_{act} production</u>

The production rate of the $N_{\mbox{\scriptsize act}}$ nuclei is given by the formula:

$$\frac{dN_{act}}{dt} = \sigma f(t) (N_T - N_{act}) - \lambda N_{act}$$

where the term: $\sigma * f(t) * (N_T - N_{act})$ describes their production during irradiation and the term $-\lambda N_{act}$ describes their simultaneous decay.

In equivalence:
$$\frac{dN_{act}}{dt} = \sigma f(t) N_T - \lambda N_{act} , \text{ because } N_T - N_{act} \approx N_T$$

The above differential equation has the following solution:

$$\frac{dN_{act}}{dt} = \sigma f(t) N_T - \lambda N_{act} \iff$$

$$\frac{dN_{act}}{dt} e^{\lambda t} = \sigma f(t) N_T e^{\lambda t} - \lambda N_{act} e^{\lambda t} \iff$$

$$\frac{dN_{act}}{dt} e^{\lambda t} + \lambda N_{act} e^{\lambda t} = \sigma f(t) N_T e^{\lambda t} \iff$$

$$\frac{dN_{act}}{dt}e^{\lambda t} + N_{act}\frac{de^{\lambda t}}{dt} = \sigma f(t)N_T e^{\lambda t} \Longleftrightarrow$$

$$d\frac{\left(N_{act}e^{\lambda t}\right)}{dt} = \sigma f(t) N_T e^{\lambda t} \Longleftrightarrow$$

By integrating from t=0 (start of irradiation, $N_{\rm act}(0)$ =0) until t=t_{\rm ir}(end of irradiation):

$$\int_{0}^{t_{ir}} d\frac{\left(N_{act}e^{\lambda t}\right)}{dt} dt = \int_{0}^{t_{ir}} \sigma f(t) N_{T}e^{\lambda t} dt \Longrightarrow$$
$$N_{act}e^{\lambda t_{ir}} = \int_{0}^{t_{ir}} \sigma f(t) N_{T}e^{\lambda t} dt \Longrightarrow$$
$$N_{act} = \frac{\sigma N_{T}\int_{0}^{t_{ir}} f(t)e^{\lambda t} dt}{e^{\lambda t_{ir}}} \Longleftrightarrow$$

$$N_{act} = \sigma N_T \left(\int_0^{t_{ir}} f(t) e^{\lambda t} dt \right) e^{-\lambda t} \iff$$

$$N_{act} = \sigma N_T \left(\int_{0}^{t_{ir}} f(t) e^{\lambda t} dt \right) \frac{\int_{0}^{t_{ir}} f(t) dt}{\int_{0}^{t_{ir}} f(t) dt} e^{-\lambda t_{ir}}$$

The integral : $\int_{0}^{t_{tr}} f(t) dt$ is the total neutron flux Φ during the irradiation:

$$N_{act} = \sigma N_T \Phi e^{-\lambda t_{ir}} \frac{\int_{0}^{t_{ir}} f(t) e^{\lambda t} dt}{\int_{0}^{t_{ir}} f(t) dt} \Longleftrightarrow$$

$$N_{act} = \sigma N_T \Phi f_b \quad (1) \text{, where } f_b = \frac{\int_0^{t_{ir}} f(t) e^{\lambda t} dt}{\int_0^{t_{ir}} f(t) dt} e^{-\lambda t_{ir}}$$

• $\underline{N_{act}} \underline{decay}$

The cps (counts per second) which the detector records are calculated via the formula:

$$cps = \frac{dN}{dt} \varepsilon I$$

$$cps = \lambda N \varepsilon I \iff \left(\frac{dN}{dt} = \lambda N \right)$$

$$cps = \lambda N_0 e^{-\lambda t} \varepsilon I \iff \left(N = N_0 e^{-\lambda t} \right)$$

By integrating from t=0 (start measurement) until t=t $_m$ (stop measurement):

$$counts = \int_{0}^{t_{m}} (\lambda N_{0} e^{-\lambda t} \varepsilon I) dt \Longrightarrow$$
$$counts = \lambda \varepsilon I N_{0} \int_{0}^{t_{m}} e^{-\lambda t} \Longleftrightarrow$$
$$counts = \varepsilon I N_{0} (1 - e^{-\lambda t_{m}})$$

where $N_0 = N_{act} e^{-\lambda t_w}$, as some N_{act} decayed after the end of the irradiation and before the detection start (waiting time).

Finally,
$$counts = \varepsilon I N_{act} e^{-\lambda t_w} (1 - e^{-\lambda t_m})$$
 (2)

By combining the equations (1) & (2) the cross section formula results:

$$\sigma = \frac{counts}{\Phi I \varepsilon N_T e^{-\lambda t_w} (1 - e^{-\lambda t_m}) f_b}$$

Appendix B

Decay during irradiation correction factor calculation program in C++ code

include <iostream> # include <cmath> # include <fstream> using namespace std; int main () { char filename[20]; double half_life; double lamda; double Irradiation_time; double dt; double flux[5000]; double sum_1=0., sum_2=0.; int number_of_channels; cout<<"give the half life in seconds: "; cin>>half_life; lamda=log(2)/half_life; cout<<"give the name of the BF3 file: "; cin>>filename; cout<<"give the number of channels: ";</pre> cin>>number_of_channels; cout<<"give the dt of each channel: "; cin>>dt; Irradiation_time=number_of_channels*dt; double fb; ifstream infile; infile.open(filename); for (int i=0;i<number of channels;i++){ infile>>flux[i]; } for(int j=0;j<number_of_channels;j++){</pre> sum_2=sum_2+flux[j]; $sum_1 = sum_1 + flux[j]^*(exp((j+1)*lamda*dt) - exp((j)*lamda*dt));$ } fb=(exp(-lamda*Irradiation_time)/(lamda*dt))*(sum_1/sum_2); cout<<"the correction factor for non constant flux is: "; cout<<fb<<"\n"; }

Appendix C

Geant4 MC simulation code for Self-Attenuation correction factor

The above Geant4 MC simulation code contains the geometry of the HPGe detector and the materials the 161 Er source consists of when it is extended and when it is assumed point.

// Canberra Reverse-Electrode Coaxial Ge Detector GR 2018

#include "XriDetectorConstruction.hh"
#include "G4SDManager.hh"
#include "G4Element.hh"
#include "G4Material.hh"
#include "G4Box.hh"
#include "G4Tubs.hh"
#include "G4Cons.hh"
#include "G4LogicalVolume.hh"
#include "G4PVPlacement.hh"

#include "G4UnitsTable.hh"
#include "globals.hh"

#include "G4SystemOfUnits.hh"
#include "G4PhysicalConstants.hh"

#include "G4VisAttributes.hh"
#include "G4Colour.hh"

#include "G4SystemOfUnits.hh"
#include "G4PhysicalConstants.hh"

XriDetectorConstruction::XriDetectorConstruction()
{;}

XriDetectorConstruction::~XriDetectorConstruction()
{;}

G4VPhysicalVolume* XriDetectorConstruction::Construct() {

G4UnitDefinition::BuildUnitsTable();

//====== materials

G4double a; G4double z; G4int iz, in;

G4double density; G4String name, symbol; G4int ncomponents; G4double fractionmass; G4int natoms; // ----- plexiglass of Eu source a = 12.011*g/mole;G4Element* elC = new G4Element(name="Carbon",symbol=" C", z= 6., a); a = 1.008*g/mole;G4Element *elH = new G4Element(name="Hydrogen", symbol=" H", z= 1., a); a = 15.999 * g/mole;G4Element *elO = new G4Element(name="Oxygen", symbol=" O", z= 8., a); // ERBIUM TARGET a=167.259*g/mole; G4Element *elEr = new G4Element(name="Erbium", symbol="Er", z= 68., a); density = 8.64 *g/cm3; G4Material* Er2O3 = new G4Material(name="Erbium_oxide",density,ncomponents=2); Er2O3->AddElement(elEr, natoms=2); Er2O3->AddElement(elO, natoms=3); density = 1.5*g/cm3; G4Material* Cellulose = new G4Material("Cellulose", density, ncomponents=3); Cellulose->AddElement(elH, natoms=10); Cellulose->AddElement(elC, natoms=6); Cellulose->AddElement(elO, natoms=5); density = 3.9*g/cm3; G4Material* ErTarget = new G4Material(name="ErTarget",density,ncomponents=2); ErTarget->AddMaterial(Cellulose,fractionmass=9.1*perCent); ErTarget->AddMaterial(Er2O3,fractionmass=90.9*perCent); /* //POINT SOURCE density = 1.19*g/cm3; G4Material* Plexiglass = new G4Material(name="Plexiglass",density,ncomponents=3); Plexiglass->AddElement(elC, natoms=5); Plexiglass->AddElement(elH, natoms=8); Plexiglass->AddElement(elO, natoms=2); */ // ----- defining Ge crystal

a = 72.61*g/mole; density = 5.323*g/cm3; G4Material* Ge = new G4Material(name="Ge",z=32., a, density); // ----- defining Mg housing

a = 24.305*g/mole; density = 1.738*g/cm3; G4Material* Mg = new G4Material(name="Mg", z=12., a, density);

// ----- defining Al housing

a = 26.981539*g/mole; density = 2.70*g/cm3; G4Material* Al = new G4Material(name="Al", z=13., a, density);

//----- defining Air

a = 14.007*g/mole; G4Element* elN = new G4Element(name="Nitrogen",symbol=" N", z= 7., a);

// a = 15.999*g/mole; // G4Element *elO = new G4Element(name="Oxygen", symbol=" O", z= 8., a);

density = 1.29*mg/cm3; G4Material *Air = new G4Material(name="Air ",density,ncomponents=2); Air->AddElement(elO, fractionmass=30.0*perCent); Air->AddElement(elN, fractionmass=70.0*perCent);

// ----- defining vacuum

G4double pressure, temperature; density = universe_mean_density; pressure = 3.0E-18*pascal; temperature = 2.73*kelvin; G4Material *Vacuum = new G4Material(name="Vacuum", z=1.0, a=1.01*g/mole, density, kStateGas, temperature, pressure);

G4cout << "\n\n ####------#### \n"; G4cout << "\n\t\t#### List of isotopes used #### \n"; // G4cout << *(G4Isotope::GetIsotopeTable()); G4cout << "\n\n\n\t\t #### List of elements used #### \n"; G4cout << *(G4Element::GetElementTable()); G4cout << "\n\n\n\t\t #### List of materials used #### \n"; G4cout << *(G4Material::GetMaterialTable()); G4cout << *(G4Material::GetMaterialTable());

//----- beam line along z axis

```
G4double startFi = 0.0^{*}deg;
 G4double endFi = 360.0*deg;
//----- world volume
 G4double WorldOutR = 20.0*cm;
 G4double WorldInR = 0.0*cm;
 G4double WorldHalfh = 30.0*cm;
 G4Tubs *World_tub
  = new G4Tubs("World_tub",WorldInR,WorldOutR,WorldHalfh,
                         startFi,endFi);
 G4LogicalVolume *World log
  = new G4LogicalVolume(World_tub,Air,"World_log",0,0,0);
 G4VPhysicalVolume *World_phys
  = new G4PVPlacement(0,G4ThreeVector(),"World",
            World log,0,false,0);
//----- Mg entrance window
 G4double SD = 1.75*cm;//1.75*cm; // SD=Source-Detector distance, set equal to 7cm+0.5mm to the
source centre
 G4double MgWOutR = 4.5*cm;
 G4double MgWInR = 0.*cm;
 G4double MgWHalfh = (1.5/2)*mm;
 G4Tubs *MgW_tube
  = new G4Tubs("MgW_tube",MgWInR,MgWOutR,MgWHalfh,
                         startFi,endFi);
 G4LogicalVolume *MgW_log
  = new G4LogicalVolume(MgW_tube,Mg,"MgW_log",0,0,0);
 G4double Pos_x = 0.0*cm;
 G4double Pos_y = 0.0*cm;
 G4double Pos_z = -SD-MgWHalfh;
 G4VPhysicalVolume *MgWTube_phys
  = new G4PVPlacement(0,
       G4ThreeVector(Pos_x,Pos_y,Pos_z),
      MgW_log,"MgWTube",World_log,false,0);
//----- Mg entrance window 2
 G4LogicalVolume *MgW_log2
```

```
= new G4LogicalVolume(MgW_tube,Mg,"MgW_log2",0,0,0);
```

 $Pos_x = 0.0*cm;$

```
Pos_y = 0.0*cm;
Pos_z = SD+MgWHalfh;
G4VPhysicalVolume *MgWTube_phys2
= new G4PVPlacement(0,
G4ThreeVector(Pos_x,Pos_y,Pos_z),
MgW_log2,"MgWTube2",World_log,false,0);
```

//----- Mg housing

G4double MgThickness = 1.5*mm; G4double MgOutR = MgWOutR; G4double MgInR = 0.*cm; G4double MgHalfh = (16.4/2.)*cm;

G4Tubs *Mg_tube = new G4Tubs("Mg_tube",MgInR,MgOutR,MgHalfh, startFi,endFi);

G4LogicalVolume *Mg_log = new G4LogicalVolume(Mg_tube,Mg,"Mg_log",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = -SD-2.*MgWHalfh-MgHalfh; G4VPhysicalVolume *MgTube_phys = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Mg_log,"MgTube",World_log,false,0);

//----- Mg housing 2

G4LogicalVolume *Mg_log2 = new G4LogicalVolume(Mg_tube,Mg,"Mg_log2",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = SD+2.*MgWHalfh+MgHalfh; G4VPhysicalVolume *MgTube_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Mg_log2,"MgTube2",World_log,false,0);

//----- Vacuum between Mg window and Mg housing

G4double VacuumOutR = MgOutR - MgThickness; G4double VacuumInR = 0.*cm; G4double VacuumHalfh = MgHalfh - MgThickness/2.; G4Tubs *Vacuum_tube = new G4Tubs("Vacuum_tube",VacuumInR,VacuumOutR,VacuumHalfh, startFi,endFi);

G4LogicalVolume *Vacuum_log = new G4LogicalVolume(Vacuum_tube,Vacuum,"Vacuum_log",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = MgThickness/2.; G4VPhysicalVolume *VacuumTube_phys = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Vacuum_log,"VacuumTube",Mg_log,false,0);

//----- Vacuum between Mg window2 and Mg housing2

```
G4LogicalVolume *Vacuum_log2
= new G4LogicalVolume(Vacuum_tube,Vacuum,"Vacuum_log2",0,0,0);
```

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = -MgThickness/2.; G4VPhysicalVolume *VacuumTube_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Vacuum_log2,"VacuumTube2",Mg_log2,false,0);

//----- Al mylar entrance window

G4double gapMg_Al = 3.95*mm; G4double AlWOutR = 3.956*cm; G4double AlWInR = 0.*cm; G4double AlWHalfh = (0.05/2)*mm;

G4Tubs *AlW_tube = new G4Tubs("AlW_tube",AlWInR,AlWOutR,AlWHalfh, startFi,endFi);

G4LogicalVolume *AlW_log = new G4LogicalVolume(AlW_tube,Al,"AlW_log",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = VacuumHalfh-gapMg_Al-AlWHalfh; G4VPhysicalVolume *AlWTube_phys = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), AlW_log,"AlWTube",Vacuum_log,false,0); //----- Al mylar entrance window2

G4LogicalVolume *AlW_log2 = new G4LogicalVolume(AlW_tube,Al,"AlW_log2",0,0,0);

```
Pos_x = 0.0*cm;
Pos_y = 0.0*cm;
Pos_z = -(VacuumHalfh-gapMg_Al-AlWHalfh);
G4VPhysicalVolume *AlWTube_phys2
= new G4PVPlacement(0,
G4ThreeVector(Pos_x,Pos_y,Pos_z),
AlW_log2,"AlWTube2",Vacuum_log2,false,0);
```

//----- Al housing

G4double AlThickness = 0.76*mm; G4double AlOutR = AlWOutR; G4double AlInR = 0.*cm; G4double AlHalfh = (12.68/2.)*cm;

G4Tubs *Al_tube = new G4Tubs("Al_tube",AlInR,AlOutR,AlHalfh, startFi,endFi);

G4LogicalVolume *Al_log = new G4LogicalVolume(Al_tube,Al,"Al_log",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = VacuumHalfh-gapMg_Al-2*AlWHalfh - AlHalfh; G4VPhysicalVolume *AlTube_phys = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Al_log,"AlTube",Vacuum_log,false,0);

//----- Al housing2

G4LogicalVolume *Al_log2 = new G4LogicalVolume(Al_tube,Al,"Al_log2",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = -(VacuumHalfh-gapMg_Al-2*AlWHalfh - AlHalfh); G4VPhysicalVolume *AlTube_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Al_log2,"AlTube2",Vacuum_log2,false,0); Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = AlThickness/2.; G4VPhysicalVolume *InVacuumTube_phys = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), InVacuum_log,"InVacuumTube",Al_log,false,0);

//----- Vacuum between Al window2 and Al housing2

G4LogicalVolume *InVacuum_log2 = new G4LogicalVolume(InVacuum_tube,Vacuum,"InVacuum_log2",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = -AlThickness/2.; G4VPhysicalVolume *InVacuumTube_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), InVacuum_log2,"InVacuumTube2",Al_log2,false,0);

//----- Dead layer Window Ge cone front

G4double FDLWConeRadiusUpMax = 3.58 *cm; //Front Dead Layer Window Uppper Max Radius G4double FDLWConeRadiusUpMin = 0.0 *cm; //Front Dead Layer Window Uppper Min Radius G4double FDLWConeRadiusBottomMax = 3.68 *cm; //Front Dead Layer Window Bottom Max Radius G4double FDLWConeRadiusBottomMin = 0.0 *cm; //Front Dead Layer Window Bottom Min Radius G4double FDLWConeHalfHeight = (0.00003/2.0)*cm; //Front Dead Layer thinkness

G4Cons *FDLW_cone = new G4Cons("FDLW_cone", FDLWConeRadiusBottomMin, FDLWConeRadiusBottomMax, FDLWConeRadiusUpMin,FDLWConeRadiusUpMax, FDLWConeHalfHeight, startFi,endFi); G4LogicalVolume *FDLW_log = new G4LogicalVolume(FDLW_cone,Ge,"FDLW_log",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = InVacuumHalfh-FDLWConeHalfHeight; G4VPhysicalVolume *FDLWCone_phys = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), FDLW_log,"FDLWCone",InVacuum_log,false,0);

//----- Dead layer Window2 Ge cone front

G4double FDLWConeRadiusUpMax2 = 3.68 *cm; //Front Dead Layer Window Uppper Max Radius G4double FDLWConeRadiusUpMin2 = 0.0 *cm; //Front Dead Layer Window Uppper Min Radius G4double FDLWConeRadiusBottomMax2 = 3.58 *cm; //Front Dead Layer Window Bottom Max Radius G4double FDLWConeRadiusBottomMin2 = 0.0 *cm; //Front Dead Layer Window Bottom Min Radius G4double FDLWConeHalfHeight2 = (0.00003/2.0)*cm; //Front Dead Layer thinkness

G4Cons *FDLW_cone2

= new G4Cons("FDLW_cone2", FDLWConeRadiusBottomMin2, FDLWConeRadiusBottomMax2, FDLWConeRadiusUpMin2,FDLWConeRadiusUpMax2, FDLWConeHalfHeight2, startFi,endFi);

G4LogicalVolume *FDLW_log2 = new G4LogicalVolume(FDLW_cone2,Ge,"FDLW_log2",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = -(InVacuumHalfh-FDLWConeHalfHeight2); G4VPhysicalVolume *FDLWCone_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), FDLW_log2,"FDLWCone2",InVacuum_log2,false,0);

//----- Front Ge cone

G4double FrontGeConeRadiusUpMax = 3.68 *cm; // Ge cone upper max radius G4double FrontGeConeRadiusUpMin = 0.0 *cm; // Ge cone upper min radius G4double FrontGeConeRadiusBottomMax = 3.78 *cm; // Ge cone bottom max radius G4double FrontGeConeRadiusBottomMin = 0.0 *cm; // Ge cone bottom min radius G4double FrontGeConeHalfHeight = (0.1/2.0)*cm; //Front Dead Layer thinkness

```
G4Cons *frontGe_cone
```

```
= new G4Cons("frontGe_cone",FrontGeConeRadiusBottomMin, FrontGeConeRadiusBottomMax,
FrontGeConeRadiusUpMin,FrontGeConeRadiusUpMax,
FrontGeConeHalfHeight,
startFi,endFi);
```

```
G4LogicalVolume *frontGeCone_log
= new G4LogicalVolume(frontGe_cone,Ge,"frontGeCone_log",0,0,0);
```

```
Pos_x = 0.0*cm;

Pos_y = 0.0*cm;

Pos_z = InVacuumHalfh-2*FDLWConeHalfHeight-FrontGeConeHalfHeight;

G4VPhysicalVolume *frontGeCone_phys

= new G4PVPlacement(0,

G4ThreeVector(Pos_x,Pos_y,Pos_z),

frontGeCone_log,"frontGeCone",InVacuum_log,false,0);
```

//----- Front Ge cone2

G4double FrontGeConeRadiusUpMax2 = 3.78 *cm; // Ge cone upper max radius G4double FrontGeConeRadiusUpMin2 = 0.0 *cm; // Ge cone upper min radius G4double FrontGeConeRadiusBottomMax2 = 3.68 *cm; // Ge cone bottom max radius G4double FrontGeConeRadiusBottomMin2 = 0.0 *cm; // Ge cone bottom min radius G4double FrontGeConeHalfHeight2 = (0.1/2.0)*cm; //Front Dead Layer thinkness

G4Cons *frontGe_cone2

= new G4Cons("frontGe_cone2",FrontGeConeRadiusBottomMin2, FrontGeConeRadiusBottomMax2, FrontGeConeRadiusUpMin2,FrontGeConeRadiusUpMax2, FrontGeConeHalfHeight2, startFi,endFi);

G4LogicalVolume *frontGeCone_log2 = new G4LogicalVolume(frontGe_cone2,Ge,"frontGeCone_log2",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = -(InVacuumHalfh-2*FDLWConeHalfHeight2-FrontGeConeHalfHeight2); G4VPhysicalVolume *frontGeCone_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), frontGeCone_log2,"frontGeCone2",InVacuum_log2,false,0);

// ----- Plexiglass or target

G4double PlexiOutR = 1.295/2.*cm;//2.0/2.*cm; G4double PlexiInR = 0.*cm; G4double PlexiHalfh = 0.2/2.*cm;

G4Tubs *Plexi_tube = new G4Tubs("Plexi_tube",PlexiInR,PlexiOutR,PlexiHalfh, startFi,endFi); G4LogicalVolume *Plexi_log = new G4LogicalVolume(Plexi_tube,ErTarget,"Plexi_log",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = 0.0*cm; //Here Christine had: -PlexiHalfh/2.; G4VPhysicalVolume *PlexiTube_phys = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Plexi_log,"PlexiTube",World_log,false,0);

//----- Dead layer of crystal at the crystal sides: denoted as "outDead"

G4double GeOutR = 3.77997*cm; //***HTAN 50/2* G4double GeHalfh = 8.99/2.*cm; G4double outDeadThickness = 0.00003*cm; G4double outDeadOutR = GeOutR + outDeadThickness; G4double outDeadInR = 0.*mm; G4double outDeadHalfh = GeHalfh;

G4Tubs *outDead_tube = new G4Tubs("outDead_tube",outDeadInR,outDeadOutR,outDeadHalfh, startFi,endFi);

G4LogicalVolume *outDead_log = new G4LogicalVolume(outDead_tube,Ge,"outDead_log",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z =InVacuumHalfh-2*FDLWConeHalfHeight-2*FrontGeConeHalfHeight-outDeadHalfh;

```
G4VPhysicalVolume *outDeadTube_phys
= new G4PVPlacement(0,
G4ThreeVector(Pos_x,Pos_y,Pos_z),
outDead_log,"outDeadTube",InVacuum_log,false,0);
```

//----- Dead layer 2 of crystal at the crystal sides: denoted as "outDead2"

G4LogicalVolume *outDead_log2 = new G4LogicalVolume(outDead_tube,Ge,"outDead_log2",0,0,0);

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z =-(InVacuumHalfh-2*FDLWConeHalfHeight2-2*FrontGeConeHalfHeight2-outDeadHalfh);

```
G4VPhysicalVolume *outDeadTube_phys2
 = new G4PVPlacement(0,
      G4ThreeVector(Pos_x,Pos_y,Pos_z),
      outDead_log2,"outDeadTube2",InVacuum_log2,false,0);
//----- Ge crystal
 G4double GeInR = 0.*mm;
 G4Tubs *Ge_tube
  = new G4Tubs("Ge_tube",GeInR,GeOutR,GeHalfh,
                          startFi,endFi);
 G4LogicalVolume *Ge_log
  = new G4LogicalVolume(Ge_tube,Ge,"Ge_log",0,0,0);
 Pos_x = 0.0*cm;
 Pos_y = 0.0^{*}cm;
 Pos_z = 0.0^{*}cm;
 G4VPhysicalVolume *GeTube_phys
  = new G4PVPlacement(0,
       G4ThreeVector(Pos_x,Pos_y,Pos_z),
       Ge_log,"GeTube",outDead_log,false,0);
//----- Ge crystal 2
```

```
G4LogicalVolume *Ge_log2
= new G4LogicalVolume(Ge_tube,Ge,"Ge_log2",0,0,0);
```

Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z = 0.0*cm; G4VPhysicalVolume *GeTube_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Ge_log2,"GeTube2",outDead_log2,false,0);

//----- Dead layer in borehole: denoted as in Dead

```
G4double BoreholeHalfh = 84/2.*mm;
G4double BoreholeOutR = 10.1/2.*mm;
G4double inDeadThickness =0.7*mm;
G4double inDeadOutR = BoreholeOutR + inDeadThickness;
G4double inDeadInR = 0.*mm;
G4double inDeadHalfh = BoreholeHalfh + inDeadThickness/2.;
```

G4Tubs *inDead_tube = new G4Tubs("inDead_tube",inDeadInR,inDeadOutR,inDeadHalfh, startFi,endFi); G4LogicalVolume *inDead_log = new G4LogicalVolume(inDead_tube,Ge,"inDead_log",0,0,0);

```
Pos_x = 0.0*cm;

Pos_y = 0.0*cm;

Pos_z = - GeHalfh + inDeadHalfh;

G4VPhysicalVolume *inDeadTube_phys

= new G4PVPlacement(0,

G4ThreeVector(Pos_x,Pos_y,Pos_z),

inDead_log,"inDeadTube",Ge_log,false,0);
```

//----- Dead layer 2 in borehole 2: denoted as inDead2

```
G4LogicalVolume *inDead_log2
= new G4LogicalVolume(inDead_tube,Ge,"inDead_log2",0,0,0);
```

```
Pos_x = 0.0*cm;

Pos_y = 0.0*cm;

Pos_z = -(- GeHalfh + inDeadHalfh);

G4VPhysicalVolume *inDeadTube_phys2

= new G4PVPlacement(0,

G4ThreeVector(Pos_x,Pos_y,Pos_z),

inDead_log2,"inDeadTube2",Ge_log2,false,0);
```

//----- Borehole

```
G4double BoreholeInR = 0.*mm;
```

G4Tubs *Borehole_tube = new G4Tubs("Borehole_tube",BoreholeInR,BoreholeOutR,BoreholeHalfh, startFi,endFi);

G4LogicalVolume *Borehole_log = new G4LogicalVolume(Borehole_tube,Vacuum,"Borehole_log",0,0,0);

```
Pos_x = 0.0*cm;

Pos_y = 0.0*cm;

Pos_z = - inDeadThickness/2.;

G4VPhysicalVolume *BoreholeTube_phys

= new G4PVPlacement(0,

G4ThreeVector(Pos_x,Pos_y,Pos_z),

Borehole_log,"BoreholeTube",inDead_log,false,0);
```

//----- Borehole 2

G4LogicalVolume *Borehole_log2 = new G4LogicalVolume(Borehole_tube,Vacuum,"Borehole_log2",0,0,0);
Pos_x = 0.0*cm; Pos_y = 0.0*cm; Pos_z =-(- inDeadThickness/2.); G4VPhysicalVolume *BoreholeTube_phys2 = new G4PVPlacement(0, G4ThreeVector(Pos_x,Pos_y,Pos_z), Borehole_log2,"BoreholeTube2",inDead_log2,false,0);

//======Visualization attributes

World log->SetVisAttributes (G4VisAttributes::Invisible); G4VisAttributes *MgWTubeAttr = new G4VisAttributes(G4Colour(0.,0.,1.)); //Blue G4VisAttributes *AlWTubeAttr = new G4VisAttributes(G4Colour(0.,0.,1.)); //Blue G4VisAttributes *MgTubeAttr = new G4VisAttributes(G4Colour(1.,0.,0.)); //Red G4VisAttributes *AlTubeAttr = new G4VisAttributes(G4Colour(1.,0.,0.)); //Red G4VisAttributes *VacuumTubeAttr = new G4VisAttributes(G4Colour(0.3,0.3,0.3)); //light gray G4VisAttributes *InVacuumTubeAttr = new G4VisAttributes(G4Colour(0.3,0.3,0.3)); //light gray G4VisAttributes *outDeadTubeAttr = new G4VisAttributes(G4Colour(0.,1.,0.)); //green G4VisAttributes *GeTubeAttr = new G4VisAttributes(G4Colour(0.8,0.8,0.8)); //grey G4VisAttributes *inDeadTubeAttr = new G4VisAttributes(G4Colour(0.,0.4,0.3)); //tale G4VisAttributes *BoreholeTubeAttr = new G4VisAttributes(G4Colour(0.,0.,1.)); //blue G4VisAttributes *PlexiTubeAttr = new G4VisAttributes(G4Colour(0.8, 0.8, 1.)); //gray // G4VisAttributes *VerticalPbAttr = new G4VisAttributes(G4Colour(1.,1.,1.)); // G4VisAttributes *HorizontalPbAttr = new G4VisAttributes(G4Colour(1.,1.,1.)); G4VisAttributes *FDLWConeAttr = new G4VisAttributes(G4Colour(0.,1.,0.)); //gree G4VisAttributes *FrontGeConeAttr = new G4VisAttributes(G4Colour(0.,1.,0.)); //gree /* VerticalPbAttr->SetVisibility(true); VerticalPbAttr->SetForceWireframe(true); vertPb_log->SetVisAttributes(VerticalPbAttr);

HorizontalPbAttr->SetVisibility(true); HorizontalPbAttr->SetForceWireframe(true); horPb_log->SetVisAttributes(HorizontalPbAttr); */

PlexiTubeAttr->SetVisibility(true); PlexiTubeAttr->SetForceWireframe(true); Plexi_log->SetVisAttributes(PlexiTubeAttr);

MgWTubeAttr->SetVisibility(true); MgWTubeAttr->SetForceWireframe(true); MgW_log->SetVisAttributes(MgWTubeAttr); MgW_log2->SetVisAttributes(MgWTubeAttr);

MgTubeAttr->SetVisibility(true); MgTubeAttr->SetForceWireframe(true); Mg_log->SetVisAttributes(MgTubeAttr); Mg_log2->SetVisAttributes(MgTubeAttr);

AlTubeAttr->SetVisibility(true); AlTubeAttr->SetForceWireframe(true); Al_log->SetVisAttributes(AlTubeAttr); Al_log2->SetVisAttributes(AlTubeAttr);

AlWTubeAttr->SetVisibility(true); AlWTubeAttr->SetForceWireframe(true); AlW_log->SetVisAttributes(AlWTubeAttr); AlW_log2->SetVisAttributes(AlWTubeAttr);

VacuumTubeAttr->SetVisibility(true); VacuumTubeAttr->SetForceWireframe(true); Vacuum_log->SetVisAttributes(VacuumTubeAttr); Vacuum_log2->SetVisAttributes(VacuumTubeAttr);

InVacuumTubeAttr->SetVisibility(true); InVacuumTubeAttr->SetForceWireframe(true); InVacuum_log->SetVisAttributes(InVacuumTubeAttr); InVacuum_log2->SetVisAttributes(InVacuumTubeAttr);

FDLWConeAttr->SetVisibility(true); FDLWConeAttr->SetForceWireframe(true); FDLW_log->SetVisAttributes(FDLWConeAttr); FDLW_log2->SetVisAttributes(FDLWConeAttr);

FrontGeConeAttr->SetVisibility(true);
FrontGeConeAttr->SetForceWireframe(true);
frontGeCone_log->SetVisAttributes(FrontGeConeAttr);
frontGeCone_log2->SetVisAttributes(FrontGeConeAttr);

outDeadTubeAttr->SetVisibility(true); outDeadTubeAttr->SetForceWireframe(true); outDead_log->SetVisAttributes(outDeadTubeAttr); outDead_log2->SetVisAttributes(outDeadTubeAttr);

GeTubeAttr->SetVisibility(true); GeTubeAttr->SetForceWireframe(true); Ge_log->SetVisAttributes(GeTubeAttr); Ge_log2->SetVisAttributes(GeTubeAttr);

inDeadTubeAttr->SetVisibility(true); inDeadTubeAttr->SetForceWireframe(true); inDead_log->SetVisAttributes(inDeadTubeAttr); inDead_log2->SetVisAttributes(inDeadTubeAttr);

BoreholeTubeAttr->SetVisibility(true); BoreholeTubeAttr->SetForceWireframe(true); Borehole_log->SetVisAttributes(BoreholeTubeAttr); Borehole_log2->SetVisAttributes(BoreholeTubeAttr); return World_phys;

}

References

- [1] Keiichi Shibata, Journal of Nuclear Science and Technology, 49, 824–835, (2012)
- [2] Generation-IV International Forum, www.gen-4.org
- [3] N. Dzysiuk, A. Kadenko, I. Kadenko, and G. Primenko, Phys. Rev. C. 86, 034609 (2012)
- [4] Junhua Luo, Rong Liu, Li Jiang, Zhenlai Liu, Journal of Radioanalytical and Nuclear Chemistry 289, 1 (2011)
- [5] Xiangzhong Kong, Yongchang Wang, Jingkang Yang, Applied Radiation and Isotopes 49, 12 (1998)
- [6] H. Liljavirta and T. Tuurnala, Physica Scripta 18, 2 (1978)
- [7] S. M. Qaim, Nuclear Physics A 224, 2 (1974)
- [8] P.Rama Prasad, J. Rama Rao, and E. Kondaiah, Nuclear Physics A 125, 1 (1969)
- [9] N. Lakshmana Das, C. V. Srinivasa Rao, B. V. Thirumala Rao, J. Rama Rao, Pramana 17, 1 (1981)
- [10] E. Havlik, Acta Phys. Austr. 34, 209 (1971)
- [11] T. Bari, Dissertation Abstracts B 32, 5091 (1972)
- [12] Εισαγωγή στις Πυρηνικέ ς Αντιδρά σει G.R. Satchler, Μετά φραση Ν Νικολή ς Εκδό σεις Πελεκά νος
- [13] N. Patronis et al, Phys. Rev. C 69, 025803 (2004)
- [14] Measurement and Detection Radiation, Nicholas Tsoulfanidis, Taylor & Francis (1798)
- [15] C. W. Reich, Nuclear Data Sheets 112, 2497 (2011)
- [16] R. B. Firestone, Nuclear Data Sheets 108, 2319 (2007)
- [17] Huang Xialong, Nuclear Data Sheets 108, 1093 (2007)
- [18] Coral M. Baglin, Nuclear Data Sheets 113, 2187 (2012)
- [19] Evert Birgesson and Goran Lovestam, Software Manual, NeuSDesc-Neutron Sources Description, IRMM, 2007
- [20] Yang Dong, Huo Junde, Nuclear Data Sheets 121, 1 (2014)
- [21] M. J. Martin, Nuclear Data Sheets 114, 1497 (2013)
- [22] International Reactor Dosimetry and Fusion File IRDFF v.1.05, 09 October, 2014

Bibliography

- [1] N. Patronis, C. T. Papadopoulos, S. Galanopoulos, M. Kokkoris, G. Perdikakis, and R. Vlastou, Physical Review C 75, 034607 (2007)
- [2] Undergraduate thesis, University of Ioannina (2014), Zinovia Eleme
- [3] M.Sc. Thesis, N.T.U.A. (2013), Antigoni Kalamara
- [4] M.Sc. Thesis, N.T.U.A. (2011), Andreas Tsinganis
- [5] Neutron Cross Sections, Donald J. Hughes, Pergamon Press (1957)
- [6] Radiation Detection and Measurement, Glenn F. Knoll, John Wiley & Sons (2000)